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Energy Sustainability

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THE INFLUENCE OF RENEWABLES ON ELECTRICITY PRICE FORECASTING: A ROBUST APPROACH [*]

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ABSTRACT: In this paper a robust approach to modelling electricity spot prices is introduced. Differently from what has been recently done in the literature on electricity price forecasting, where the attention has been mainly drawn by the prediction of spikes, the focus of this contribution is on the robust estimation of nonlinear SETARX models (Self-Exciting Threshold Auto Regressive models with eXogenous regressors). In this way, parameters estimates are not, or very lightly, influenced by the presence of extreme observations and the large majority of prices, which are not spikes, could be better forecasted. A Monte Carlo study is carried out in order to select the best weighting function for Generalized M-estimators of SETAR processes. A robust procedure to select and estimate nonlinear processes for electricity prices is introduced, including robust tests for stationarity and nonlinearity and robust information criteria. The application of the procedure to the Italian electricity market reveals the forecasting superiority of the robust GM-estimator based on the polynomial weighting function respect to the non-robust Least Squares estimator. Finally, the introduction of external regressors in the robust estimation of SETARX processes contributes to the improvement of the forecasting ability of the model.

JEL Codes: C13, C15, C22, C53, Q47
Keywords: Electricity price, nonlinear time series, price forecasting, robust GM-estimator, spikes, threshold models.

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1. Introduction

Spot electricity prices are known to exhibit sudden and very large jumps to extreme levels as a consequence of sudden grid congestions, unexpected shortfalls in supply, and failures of the transmission infrastructure (Christensen et al., 2012). Such events reflect immediately on prices because of the non-storable nature of electrical energy and the requirement of a constant balance between demand and supply (Huisman & Mahieu, 2003). This feature must be considered very carefully and robust techniques must be applied to avoid that few jumps could dramatically affect parameter estimates and, consequently, forecasts.

Although many papers have applied quite sophisticated time series models to time series of electricity and gas prices and demand with spikes, only few have considered the strong influence of jumps on estimates and the need to move to robust estimators (Janczura et al., 2013; Nowotarski et al., 2013; Haldrup et al., 2016).

In the present paper we suggest to use a version of threshold autoregressive models (SETARX) where parameters are estimated robustly to the presence of spikes. Differently from what has been done in the literature so far, we are not interested in modelling spikes, but we want to focus the attention on the influence that spikes can have on the estimated coefficients. If non robust estimators are applied, coefficient could be very badly biased and even non-spiky observations, which are the very large majority, could not be properly modeled and forecasted.

Moreover, we suggest a completely robust approach to modelling and forecasting electricity prices which combines robust estimation of a SETARX model, robust tests for unit roots and nonlinear components and robust information criteria. Although we are aware of the limits of this class of models (Misiorek et al., 2006), threshold models represent a simple approach which takes into account the possible nonlinearity of electricity prices and allows the inclusion of external regressors to improve their forecasting performances (Maciejowska et al., 2016).

Threshold Auto Regressive (TAR) models are quite popular in the nonlinear time-series literature. This popularity is due to the fact that they are relatively simple to specify, estimate, and interpret. However, the issue of outliers in non-linear time series models is far from being clearly solved. From the analysis of the existing literature, it is not clear the extent of the bias of robust estimators of the threshold with respect to LS estimator, how to choose the best weighting function and the forecasting performances of different weighting functions have never been compared.

Moreover, robust estimators of regime switching processes are not implemented within the most popular software platforms among statisticians, such as Matlab and R.

Grossi & Nan (2015) have started to address the above points through a Monte Carlo experiment which compared the performances of classical SETAR estimator and robust estimator using various weighting functions. The main insights obtained from that preliminary work are confirmed in the present paper where a more extensive simulation experiment is carried out. The simulation experiment has required the implementation of all the estimators (classical and robust) in R language resulting in a set of functions which hopefully will become a library soon.

The results obtained from the simulation experiment are used to estimate the parameters of SETAR models on the Italian electricity price data (*PUN, prezzo unico nazionale*). The model is enriched by the introduction of exogenous regressors which improve the forecasting performances. Crucial variables in predicting electricity prices are dummies for the intra-weekly seasonality, predicted demanded volumes and predicted wind power generation (Gianfreda & Grossi, 2012).

Summarizing, the main contributions of the present paper are:

- a Monte Carlo simulation study is performed to integrate partial simulations done in previous papers. At the end of this study the best robust estimator is clearly detected;
- a robust approach to modelling and forecasting electricity prices is suggested which include tests, estimation of parameters and selection of the best model;
- a robust nonlinear model with exogenous regressors is estimated which takes into account the main stylized facts observed on electricity markets and includes the forecasted regressors which have revealed to increase substantially the forecasting performances (Gaillard et al., 2016; Weron, 2014).

The structure of the paper is as follows. Section 2 is dedicated to the analysis of the literature relevant in the context of robust estimation and forecasting of electricity prices. In section 3 the general SETAR model is defined and different weighting functions are used to robustify the classic estimator are discussed. Section 4 contains the main results of the Monte Carlo simulation study. The analysis of the forecasting performances of the robust SETARX model based on the polynomial weighting function is presented in section 5. Section 6 reports some concluding remarks and suggestions for future research.

2. Literature review

Forecasting electricity prices is a crucial objective for many reasons (Nogales et al., 2002). First of all, speculative trading on electricity markets has become more and more important, especially on the short-run. Strictly related to trading is the possibility to evaluate the economic convenience of short-run electricity storage facilities which would be of great importance for the strategic role they could play on the integration of intermittent renewable sources into the grid (Flatley et al., 2016). From the regulator perspective, it is of vital relevance the ability to predict future prices in order to reduce the risk of volatility and its impact on final consumers (Hong et al., 2016). Also generators are interested in future prices for driving the decision related to the capacity size of the plants and to the load to produce and inject into the grid (Aggarwal et al., 2009). With an accurate day-ahead price forecast, a producer can develop an appropriate bidding strategy to maximize ones own benefit, or a consumer can maximize its utility (Conejo et al., 2005). For a very detailed discussion of the relevance of electricity price forecasting, see Weron (2014).

As it is well known, the presence of spikes is a crucial stylized fact in electricity price time series (Gianfreda & Grossi, 2012). Several papers have dealt with the issue of modelling spikes in electricity prices. Particularly used have been diffusion processes introducing spikes through the addition of a Poisson jump component (Cartea & Figueroa, 2005; Escribano et al., 2011). Processes with heavy-tailed distributions have instead been estimated by Bystrom (2005), Panagiotelis & Smith (2008) and Swider & Weber (2007). Other authors have coped with the issue of predicting price spikes which are particularly relevant for risk management (Laouafi et al., 2016). In this context, Christensen et al. (2012) suggested a modified autoregressive conditional hazard model to predict price spikes in the Australian electricity market. Clements et al. (2013) proposed a semi-parametric model for price spikes forecasting. The necessity to resort to nonlinear time series models has been pointed out, among others, by Bordignon et al. (2013) where Markov switching models are applied to forecast prices on the UK electricity market. Other authors have applied threshold autoregressive models (Ricky Rambharat et al., 2005; Zachmann, 2013; Haldrup & Nielsen, 2006; Lucheroni, 2012; Sapio & Spagnolo, 2016) to separate a normal regime, when volatility is rather low, and a high volatility regime when spikes are observed. The superiority of regime switching models with respect to models without regimes has been argued by Janczura & Weron (2010) and Kosater & Mosler (2006), who have observed better forecasting performances for nonlinear processes. An interesting approach has been suggested recently by Gaillard et al. (2016), who predict the maximal price of the day, which is then used as an exogenous variable in a prediction model based on a quantile regression estimator.

The sampling properties of the estimators and test statistics associated with nonlinear TAR models have been studied by Tsay (1989) and Hansen (1997, 1999). In the class of non-linear models, studies addressed to robustifying this kind of models are very few, although the problem is very challenging, particularly when it is not clear whether aberrant observations must be considered as outliers or as generated by a real non-linear process. van Dijk (1999) derived an outlier robust estimation method for the parameters in Smooth Threshold Auto Regressive (STAR) models, based on the principle of generalized maximum likelihood type estimation. Battaglia & Orfei (2005) focused on outlier detection and estimation through a model-based approach when the time series is generated by a general non-linear process. A general model able to capture nonlinearity, structural changes and outliers has been introduced by Giordani et al. (2007). The authors suggest to employ the state-space framework which allows to estimate the coefficients of several non-linear time series models and simultaneously take into account the presence of outliers and structural breaks. The method seems quite effective in modeling macro-economic time series. Chan & Cheung (1994) extended the generalized M estimator method[2] to Self-Exciting Threshold Auto Regressive (SETAR) models. Their simulation results show that the GM estimation is preferable to the LS estimation in presence of additive outliers. As GM estimators have proved to be consistent with a very small loss of efficiency, at least under normal assumptions, the extension to threshold models, which are piecewise linear, looks quite straightforward. Despite this observation, a cautionary note has been written by Giordani (2006) to point out some drawbacks of the GM estimator proposed by Chan & Cheung (1994). In particular, it is argued and shown, by means of a simulation study, that the GM estimator can deliver inconsistent estimates of the threshold even under regularity conditions. According to this contribution, the inconsistency of the estimates could be particularly severe when strongly descending weight functions are used. Zhang et al. (2009) demonstrate the consistency of GM estimators of autoregressive parameters in each regime of SETAR models when the threshold is unknown. The consistency of parameters is guaranteed when the objective function is a convex non-negative function. A possible function holding these properties is the

[2]For an overview about GM estimators see (Andersen, 2008, chap. 4) and (Maronna et al., 2006, chap. 8.5)

Huber $\rho-$function which is suggested to replace the polynomial function used in Giordani's (2006) paper. However, the authors conclude, the problem of finding a threshold robust estimator with desirable finite-sample properties is still an open issue. Although a theoretical proof has been provided by the authors, there is not a well structured Monte Carlo study to assess the extent of the distortion of the GM-SETAR estimator.

3. SETAR models with exogenous regressors

Given a time series y_t, a two-regime Self-Exciting Threshold Auto Regressive model SETAR(p,d) with exogenous regressors is specified as

$$y_t = \begin{cases} \mathbf{x}_t\boldsymbol{\beta}_1 + \mathbf{z}_t\boldsymbol{\lambda}_1 + \varepsilon_{1t}, & \text{if} \quad y_{t-d} \leq \gamma \\ \mathbf{x}_t\boldsymbol{\beta}_2 + \mathbf{z}_t\boldsymbol{\lambda}_2 + \varepsilon_{2t}, & \text{if} \quad y_{t-d} > \gamma \end{cases} \tag{1}$$

for $t = \max(p, d), ..., N$, where y_{t-d} is the threshold variable with $d \geq 1$ and γ is the threshold value. The relation between y_{t-d} and γ states if y_t is observed in regime 1 or 2. $\boldsymbol{\beta}_j$ is the vector of auto-regressive parameters for regime $j = 1, 2$ and $\mathbf{x}_t$ is the t-th row of the $(N \times p)$ matrix $\mathbf{X}$ comprising p lagged variables of y_t. $\boldsymbol{\lambda}_j$ is the vector of parameters corresponding to exogenous regressors and/or dummies contained in the $(N \times r)$ matrix $\mathbf{Z}$ whose t-th row is $\mathbf{z}_t$. Errors ε_{1t} and ε_{2t} are assumed to be independent and to follow distributions $\text{iid}(0, \sigma_{\varepsilon,1})$ and $\text{iid}(0, \sigma_{\varepsilon,2})$ respectively.

3.1. Estimation of SETAR models

In general the value of the threshold γ is unknown, so that the parameters to estimate become $\boldsymbol{\theta}_1 = (\boldsymbol{\beta}_1', \lambda_1')'$, $\boldsymbol{\theta}_2 = (\boldsymbol{\beta}_2', \lambda_2')'$, γ, $\sigma_{\varepsilon,1}$ and $\sigma_{\varepsilon,2}$. Parameters can be estimated by sequential conditional least squares. For a fixed threshold γ the observations may be divided into two samples $\{y_t | y_{t-d} \leq \gamma\}$ and $\{y_t | y_{t-d} > \gamma\}$: the data can be denoted respectively as $\mathbf{y}_j = (y_{ji_1}, y_{ji_2}, ..., y_{ji_{N_j}})'$ in regimes $j = 1, 2$, with N_1 and N_2 the regimes sample sizes and $N_1 + N_2 = N - \max(p, d)$.

Parameters $\boldsymbol{\theta}_1$ and $\boldsymbol{\theta}_2$ can be estimated by OLS as

$$\hat{\boldsymbol{\theta}}_j = \left(\mathbf{X}_j^{*\prime}\mathbf{X}_j^*\right)^{-1}\mathbf{X}_j^{*\prime}\mathbf{y}_j \tag{2}$$

for $j = 1, 2$ where $\mathbf{X}_j^* = (\mathbf{X}_j, \mathbf{Z}_j) = ((\mathbf{x}_{ji_1}', ..., \mathbf{x}_{ji_{N_j}}')', (\mathbf{z}_{ji_1}', ..., \mathbf{z}_{ji_{N_j}}')')$ is the $(N_j \times (p+r))$ matrix of regressors for each regime. The variance estimates can be calculated as $\hat{\sigma}_{\varepsilon,j} = \mathbf{r}_j'\mathbf{r}_j/(N_j - (p+r))$, with $\mathbf{r}_j = \mathbf{y}_j - \mathbf{X}_j^*\hat{\boldsymbol{\theta}}_j$.

The least square estimate of γ is obtained by minimizing the joint residual sum of squares

$$\gamma = \arg\min_{\gamma\in\Gamma} \sum_{j=1}^{2} \mathbf{r}_j'\mathbf{r}_j \tag{3}$$

over a set Γ of allowable threshold values so that each regime contains at least a given fraction φ (ranging from 0.05 to 0.3) of all observations[3].

3.2. Robust estimation of SETAR models

In the case of robust two-regime SETAR model, for a fixed threshold γ the GM estimate of the autoregressive parameters can be obtained by applying the iterative weighted least squares:

$$\hat{\boldsymbol{\theta}}_j^{(n+1)} = \left(\mathbf{X}_j^{*\prime}\mathbf{W}_j^{(n)}\mathbf{X}_j^{*}\right)^{-1}\mathbf{X}_j^{*\prime}\mathbf{W}_j^{(n)}\mathbf{y}_j \tag{4}$$

where $\hat{\boldsymbol{\theta}}_j^{(n+1)}$ is the GM estimate for the parameter vector in regime $j = 1, 2$ after the n-th iteration from an initial estimate $\hat{\boldsymbol{\theta}}_j^{(0)}$, and $\mathbf{W}_j^{(n)}$ is a weight diagonal $(N_j \times N_j)$ matrix, whose elements depend on a weighting function $w(\hat{\boldsymbol{\theta}}_j^{(n)}, \hat{\sigma}_{\varepsilon,j}^{(n)})$ bounded between 0 and 1. The threshold γ can be estimated by minimizing the objective function $\rho(\mathbf{r}_1, \mathbf{r}_2)$ over the set Γ of allowable threshold values.

Different weight functions have been proposed in the literature. The first method is described in Chan & Cheung (1994). Weights are calculated as

$$w(\hat{\boldsymbol{\theta}}_j, \hat{\sigma}_{\varepsilon,j}) = \psi\left(\frac{y_t - m_{y,j}}{C_y\hat{\sigma}_{y,j}}\right)\psi\left(\frac{y_t - \mathbf{x}_t^*\hat{\boldsymbol{\theta}}_j}{C_\varepsilon\hat{\sigma}_{\varepsilon,j}}\right)$$

where $m_{y,j}$ is a robust estimate of the location parameter (sample median) in the j-th regime. $\hat{\sigma}_{y,j}$ and $\hat{\sigma}_{\varepsilon,j}$ are robust estimates of the scale parameters σ_y and σ_ε respectively, obtained by the median absolute deviation multiplied by 1.483. C_y and C_ε are tuning constants fixed at 6.0 and 3.9 respectively. In this case, ψ is the redescending Tukey bisquare weight function, defined as

$$\psi(u) = \begin{cases} (1-(u/c)^2)^2 & \text{if} \quad |u| \le c, \\ 0 & \text{if} \quad |u| > c. \end{cases}$$

[3]In order to ensures a sufficient number of observations around the true threshold parameter so that it can be identified, the value of φ is usually set between 0.10 and 0.15 (Gonzalo & Pitarakis, 2002). In the simulation study of section 4 and in the applied study of section 5 we have used a value of $\varphi = 0.15$ which make the OLS estimation of the threshold "naturally" robust and more difficult to outperform by the robust estimators. Moreover, 0.15 is the default value used by the `selectSETAR` R function of the library `tsDyn`.

where c is the tuning constant taken equal to 1 following Chan & Cheung (1994). The objective function to minimize for the search of the threshold depends on Tukey bisquare weights. We use the same function as described in Chan & Cheung (1994).

For the second method, we follow Franses & van Dijk (2000). The GM weights are presented in Schweppe's form $w(\hat{\boldsymbol{\theta}}_j, \hat{\sigma}_{\varepsilon,j}) = \psi(r_t)/r_t$ with standardized residuals $r_t = (y_t - \mathbf{x}_t^* \hat{\boldsymbol{\theta}}_j)/(\hat{\sigma}_{\varepsilon,j} w(\mathbf{x}_t^*))$ and $w(\mathbf{x}_t^*) = \psi(\mathrm{d}(\mathbf{x}_t^*)^\alpha)/\mathrm{d}(\mathbf{x}_t^*)^\alpha$. $\mathrm{d}(\mathbf{x}_t^*) = |\mathbf{x}_t^* - m_{y,j}|/\hat{\sigma}_{y,j}$ is the Mahalanobis distance and α is a constant usually set equal to 2 to obtain robustness of standard errors. The chosen weight function is the Polynomial ψ function as proposed in Lucas et al. (1996), given by

$$\psi(u) = \begin{cases} u & \text{if} \quad |u| \leq c_1, \\ \mathrm{sgn}(u) g(|u|) & \text{if} \quad c_1 < |u| \leq c_2, \\ 0 & \text{if} \quad |u| > c_2, \end{cases}$$

where $\mathrm{sgn}(u)$ is the sign function, $g(|u|)$ is a fifth-order polynomial such that $\psi(u)$ is twice continuously differentiable, and c_1 and c_2 are tuning constants, taken to be the square roots of the 0.99 and 0.999 quantiles of the $\chi^2(1)$ distribution ($c_1 = 2.576$ and $c_2 = 3.291$)[4]. The threshold γ is estimated by minimizing the objective function $\sum_{t=1}^{N} w(\hat{\boldsymbol{\theta}}, \hat{\sigma}_\varepsilon)(y_t - \mathbf{x}_t^* \hat{\boldsymbol{\theta}})^2$ over the set Γ of allowable threshold values.

The third method is based on the same methodologies as the second but with ψ the Huber weight function, given by

$$\psi(u) = \begin{cases} -c & \text{if} \quad u \leq -c, \\ u & \text{if} \quad -c < u \leq c, \\ c & \text{if} \quad u > c, \end{cases}$$

where c is a tuning constant taken equal to 1.345 to produce an estimator that has a relative efficiency of 95 per cent compared to the OLS estimator if ε_t is normally distributed.

4. Simulation experiment

In their original paper Chan & Cheung (1994) carried out a simulation study to evaluate the bias of OLS and GM estimators of SETAR parameters. The simulation experiment was based on

[4]Different values of the tunig constants have been used but results both of simulations and forecasting does not seem to be strongly influenced.

quite short time series ($N = 100$) generated from eighteen different SETAR processes. The outliers were included considering a simple pattern based on few values of the contamination parameter. Finally, they considered just the Tukey's weighting function without any comparison with other possible weighting functions. The Monte Carlo simulation performed in this paper extends the Chan & Cheung (1994)'s experiment in three directions:

- two additional sample size are considered, that is $N = 500$ and $N = 1000$;
- more complex contamination patterns are analyzed: one single outlier and three outliers for all sample sizes, multiple outliers at fixed positions and at random positions for large sample sizes ($N = 500$ and $N = 1000$).
- two new weighting functions (the Huber's and the polynomial function) are applied to obtain new robust GM estimators whose performances are compared to those of the Tukey's function.

To assess the performance of the three weighting functions, we reproduce the simulation study of Chan & Cheung (1994) using the same eighteen combinations of parameters $\boldsymbol{\theta} = (\beta_1, \beta_2, \gamma, d)$ to simulate from the same processes used by Chan & Cheung (1994)[5]. We generate time series from SETAR(1,d) models for fixed sample sizes of $N = 100, 500, 1000$, with 1000 replications respectively, and $\sigma_\varepsilon^2 = 1$.

The series are contaminated following four schemes. For the single-outlier case, applied only for series with $N = 100$, an additive outlier is located at $t = N/2$ with magnitude $\omega = 0, 3, 4, 5$ times the standard deviation of the process. For the 3-outlier case ($N = 100, 500$), we fixed three outliers at $t = N/4, N/2$, and $N * 3/4$ with magnitude $-\omega, \omega, -\omega$ respectively. The multiple-outlier case is applied only for series with $N = 500$: three outliers are fixed every 100 observations with the same scheme of the 3-outlier case. The fourth scheme is reserved to series with a sample size of $N = 1000$: a random outlier contamination obtained using a binomial distribution with the fixed probability of 4%.

For the first robust estimation method based on the Tukey's weighting function, following Chan & Cheung (1994), the starting values β_1^0, β_2^0 of the parameters are calculated by four iterations with Huber weights with OLS estimates as initial points. For the second and third method based on

[5]See Chan & Cheung (1994) for the 18 parameter combinations.

the polynomial and the Huber's function, respectively, the starting values are calculated by least median of squares[6].

In Table 1 we have summarized the results of the Monte Carlo experiment. The purpose of this table is to examine how many times each of the three robust GM estimators, called "TUK" (Tukey), "POL" (Polynomial) and "HUB" (Huber), give better estimation results of the non-robust LS estimator in terms of Root Mean Squared Error (RMSE). Three parameters (the threshold γ and the two AR parameters β_1 and β_2) are estimated on trajectories generated without contamination and with different levels of contamination ($\omega = 0, 3, 4, 5$).

The main results can be summarized as follows. When the series are not contaminated ($\omega = 0$), LS is expected to better estimate the parameters. For this reason, the RMSE of the autoregressive parameters estimated by the robust estimators is never lower than the RMSE of the LS estimator. As regards the threshold parameter, only few times the RMSE of the HUB and POL is smaller than that of the LS. According to what it has been proven by Zhang et al. (2009), the robust estimators of the threshold parameter are less efficient than the LS estimator in small samples. As a consequence, we found that all three robust methods performed generally worse than the LS, at least for weak contamination patterns, that is in the single outlier case with small magnitude ($\omega = 3$).

Increasing the sample size and the complexity of the contamination pattern, the robust estimation of the autoregressive parameters becomes increasingly better than the LS method. For instance, moving form $N = 100$ to $N = 500$ the number of times when HUB and POL estimate the autoregressive parameters better than LS varies between 14 and 17 out of 18 with a 3-outlier contamination and $\omega \geq 4$. The number of success reach the maximum value (18) when $N = 1000$ and 4% contamination is introduced (lower panel of Table 1). The same results are not shown by the TUK's estimator, whose performances are always lower than HUB and POL and many times are even worse than those of the LS estimator.

Drawing our attention on the threshold parameter (γ, first columns of Table 1), it is immediately clear that, while the method suggested by Chan & Cheung (1994) based on the Tukey function does not show any significant improvement with respect to LS, the other two methods look to be

[6] Different starting values have been chosen deliberately to keep the first method as it was originally suggested by Chan & Cheung (1994).

Table 1: *Number of cases (out of 18) RMSEs of the Robust estimation are better than RMSEs of the LS estimation. 1000 MC simulations of time series with sample sizes* $N = 100, 500, 1000$ *and different contamination patterns. First column reports the name of the weighting function.*

	$\hat{\gamma}$				$\hat{\beta}_1$				$\hat{\beta}_2$			
Case	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5
Sample size $N = 100$												
Single-outlier case												
POL	3	3	5	6	0	0	5	13	0	10	13	13
HUB	4	4	4	7	0	5	12	15	0	11	14	14
TUK	2	2	2	4	0	1	3	4	0	2	7	10
3-outlier case												
POL	2	4	6	6	0	9	14	15	0	12	14	14
HUB	3	4	6	6	0	12	15	16	0	13	14	14
TUK	2	2	2	2	0	11	11	11	0	3	11	11
Sample size $N = 500$												
3-outlier case												
POL	4	2	6	5	0	11	14	17	0	12	14	14
HUB	4	3	4	6	0	12	16	17	0	13	14	15
TUK	0	0	1	1	0	1	2	4	0	0	1	1
Multiple-outlier case												
POL	4	4	8	10	0	15	17	18	0	14	15	16
HUB	4	5	7	7	0	17	18	18	0	14	16	16
TUK	0	2	2	2	0	9	13	13	0	11	14	14
Sample size $N = 1000$												
Random outliers contamination (4%)												
POL	4	4	7	9	0	18	18	18	0	17	18	18
HUB	4	7	7	8	0	18	18	18	0	17	17	17
TUK	0	2	2	2	0	12	13	13	0	13	12	13

competitive to LS, particularly for large sample sizes and complex contamination patterns. The robust estimation of the threshold looks to be a critical issue. However, we need to remember that this parameters is intrinsically robust, even when the LS estimator is applied, because it is estimated on the central part of the distribution, after the removal of possible extreme observation in the queues of the distribution (see equation 3). Moreover, a more reliable comparison between the different estimators should quantify, not only the number of times a method is better than the other, but also the relative value of the RMSE. Such a comparison is shown in Table 2.

To give an overall idea of the results reported in Table 2, we have computed the average values of the RMSEs ratios of the robust estimators with respect to the LS estimator using all 18 simulated time series with 1000 MC simulations each with sample sizes $N = 100, 500, 1000$ and different contamination designs. For instance, the first value in Table 2 (1.301) means that the average value of the RMSE obtained on the 18 simulated time series with sample size $N = 100$ using the Polynomial weight function is 30.1% higher than the RMSE of the LS estimator when the threshold is estimated on non-contaminated trajectories in accordance to the higher efficiency of LS. Thus, values greater than 1 mean that the analyzed estimator is worse than the compared estimator. From Table 2 we can conclude that all robust estimators are overperformed by the LS estimator when the parameters are estimated on non-contaminated series ($\omega = 0$). However, the Polynomial function is the only one to overperform the LS estimator in the estimation of the threshold parameter when the magnitude of the contamination is high ($\omega \geq 4$) and/or the number of outliers is high. On the other hand, POL and HUB functions are always far better than LS in the estimation of $\beta_i, i = 1, 2$ on contaminated series. These results confirm the theoretical results provided by Zhang et al. (2009).

Once it has been shown that robust GM-estimators perform better than LS when long series are not-trivially contaminated, we need to choose which weighting function gives the most reliable estimates. To this purpose we compare the couples of weighting functions that could be created from the three considered in the present paper. Results are shown in Table 3 and Table 4. The clear preference of Polynomial and Huber functions to the Tukey weights is strongly confirmed. Moreover, Polynomial reveals to be always better than Huber function when the sample size increases and the magnitude and/or the number of outliers are high. In the other cases the two weighting functions look to perform quite similar. However, when the sample size is ≥ 500 and

Table 2: *Means of the 18 RMSEs ratios of the GM estimate to the LS estimate. 1000 MC simulations of time series with sample sizes* $N = 100, 500, 1000$ *and different contamination designs. First column reports the name of the weight function.*

	$\hat{\gamma}$				$\hat{\beta}_1$				$\hat{\beta}_2$			
Case	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5
Sample size $N = 100$												
Single-outlier case												
POL	1.301	1.252	1.173	1.121	1.321	1.176	1.088	0.998	1.381	1.204	1.038	0.951
HUB	1.229	1.174	1.155	1.096	1.191	1.079	1.025	0.935	1.252	1.077	0.963	0.866
TUK	1.753	1.65	1.588	1.48	1.648	1.488	1.394	1.242	1.733	1.437	1.305	1.201
3-outlier case												
POL	1.292	1.171	1.12	1.086	1.308	0.982	0.817	0.721	1.365	1.054	0.885	0.836
HUB	1.218	1.139	1.124	1.126	1.194	0.88	0.759	0.674	1.238	0.977	0.879	0.802
TUK	1.742	1.543	1.498	1.435	1.656	1.125	0.997	0.901	1.724	1.302	1.157	1.09
Sample size $N = 500$												
3-outlier case												
POL	1.385	1.226	1.135	1.07	1.164	0.94	0.779	0.642	1.255	1.064	0.897	0.75
HUB	1.265	1.179	1.139	1.067	1.112	0.912	0.756	0.632	1.173	1.014	0.863	0.723
TUK	4.048	3.586	3.186	2.841	3.086	2.341	1.972	1.623	3.068	2.599	2.221	1.908
Multiple-outlier case												
POL	1.371	1.088	0.948	0.885	1.158	0.612	0.42	0.33	1.253	0.67	0.481	0.392
HUB	1.278	1.073	1.02	1.007	1.115	0.611	0.451	0.366	1.173	0.667	0.513	0.444
TUK	4.152	2.939	2.384	2.079	3.085	1.109	0.869	0.765	3.121	1.485	1.202	1.057
Sample size $N = 1000$												
Random outliers contamination (4%)												
POL	1.34	0.955	0.873	0.827	1.128	0.404	0.29	0.237	1.176	0.365	0.278	0.231
HUB	1.286	1.043	1.032	1.012	1.107	0.427	0.325	0.276	1.131	0.401	0.314	0.272
TUK	6.699	4.525	3.711	2.864	4.19	1.162	0.968	0.888	4.088	1.401	1.266	1.098

the contamination pattern is complex (multiple-outlier case and random outlier contamination), the Polynomial function is better than Huber's function. In particular, looking at the bottom lines of Table 4, we can note that the ratio of the Polynomial RMSE to the Huber RMSE is always less than one, thus the Polynomial weighting function reveals to be the best robust estimator. In order to assess the performance of the Polynomial function compared to the LS estimator even in presence of strongly contaminated trajectories, Appendix A contains some tables reporting the ratio of the RMSE of the two estimators (Polynomial is the numerator) in the three-outlier case (Table A.1) and the multiple-outlier case (Table A.2). Differently from previous tables, detailed output for each generated process is reported. In most of the cases the ratio is lower than 1, so that the superiority of the polynomial on the LS estimator is confirmed. A summary of the two tables is shown in Table A.3.

As it will be discussed in section 5, series of electricity prices are usually longer than 500 times and the presence of spikes usually reproduce the most complex contamination patterns described in the present section, thus the robust GM-estimator based on the Polynomial weighting function will be used in the application.

5. Robust price forecasting on the Italian electricity market

5.1. Data description

Following the results of the simulation experiment, in this section, we apply LS and the robust POL weighting functions to estimate parameters of SETAR models on the Italian electricity price data (*PUN, prezzo unico nazionale*), downloaded from the website of the Italian electricity authority [7]. Moreover, a comparison of the prediction accuracy of the two estimators is implemented.

The time series of prices used in the present work covers the period from January 1st, 2013 to December 31th, 2015 (26,280 data points, for N = 1,095 days): year 2015 has been left for out-of-sample forecasting. The data have an hourly frequency, therefore each day consist of 24 load periods with 00:00–01:00am defined as period 1. Spot price is denoted as P_{th}, where t specifies the day and j the load period ($t = 1, 2, ..., N$; $h = 1, 2, ..., 24$).

In this study, following a widespread practice in literature (Weron, 2014), each hourly time series is modeled separately. There are at least two motivations behind this choice. First, electricity prices

[7]Gestore del Mercato Elettrico (GME), `http://www.mercatoelettrico.org/en/`

Table 3: *Number of cases (out of 18) RMSEs of the first robust method are better than RMSEs of the second method. 1000 MC simulations of time series with sample sizes* $N = 100, 500, 1000$ *and different contamination designs.*

	$\hat{\gamma}$				$\hat{\beta}_1$				$\hat{\beta}_2$			
Case	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5
Sample size $N = 100$												
Single-outlier case												
POL to HUB	5	4	7	7	0	3	3	2	2	2	5	1
POL to TUK	18	16	17	18	14	14	14	14	16	16	17	17
HUB to TUK	17	17	18	18	17	18	16	16	18	18	18	18
3-outlier case												
POL to HUB	5	6	7	15	0	4	6	7	0	2	7	8
POL to TUK	18	16	17	18	15	14	17	17	16	16	17	18
HUB to TUK	18	18	17	18	18	16	18	18	17	17	18	18
Sample size $N = 500$												
3-outlier case												
POL to HUB	4	8	11	12	3	6	8	8	2	7	5	8
POL to TUK	18	18	18	18	18	18	18	18	18	18	18	18
HUB to TUK	18	18	18	18	18	18	18	18	18	18	18	18
Multiple-outlier case												
POL to HUB	5	4	13	17	3	11	15	16	3	11	13	17
POL to TUK	18	18	18	18	18	18	18	18	18	18	18	18
HUB to TUK	18	18	18	18	18	17	18	18	18	18	18	18
Sample size $N = 1000$												
Random outliers contamination (4%)												
POL to HUB	12	15	18	18	3	16	17	18	1	17	18	18
POL to TUK	18	18	18	18	18	18	18	18	18	18	18	18
HUB to TUK	18	18	18	18	18	18	18	18	18	18	18	18

Table 4: *Means of the 18 RMSEs ratios of the GM estimation. 1000 MC simulations of time series with sample sizes* $N = 100, 500, 1000$ *and different contamination designs.*

	$\hat{\gamma}$				$\hat{\beta}_1$				$\hat{\beta}_2$			
Case	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5	$\omega = 0$	3	4	5
Sample size $N = 100$												
Single-outlier case												
POL to HUB	1.057	1.045	1.022	1.028	1.106	1.087	1.068	1.051	1.103	1.104	1.073	1.071
POL to TUK	0.795	0.792	0.789	0.793	0.825	0.813	0.815	0.817	0.804	0.824	0.778	0.744
HUB to TUK	0.764	0.764	0.778	0.777	0.748	0.747	0.763	0.776	0.728	0.744	0.722	0.692
3-outlier case												
POL to HUB	1.047	1.025	1.003	0.971	1.101	1.08	1.032	1.043	1.104	1.072	1.007	1.02
POL to TUK	0.793	0.795	0.784	0.777	0.816	0.858	0.766	0.728	0.811	0.823	0.75	0.723
HUB to TUK	0.766	0.779	0.78	0.798	0.74	0.789	0.736	0.692	0.735	0.766	0.742	0.704
Sample size $N = 500$												
3-outlier case												
POL to HUB	1.07	1.033	1.009	1.015	1.039	1.033	1.021	1.013	1.069	1.037	1.025	1.019
POL to TUK	0.52	0.512	0.51	0.509	0.436	0.472	0.462	0.446	0.442	0.449	0.436	0.43
HUB to TUK	0.504	0.509	0.517	0.52	0.423	0.459	0.451	0.437	0.412	0.436	0.425	0.426
Multiple-outlier case												
POL to HUB	1.067	1.013	0.925	0.887	1.038	0.966	0.909	0.902	1.06	0.962	0.889	0.874
POL to TUK	0.519	0.504	0.489	0.491	0.439	0.586	0.477	0.419	0.437	0.52	0.433	0.399
HUB to TUK	0.507	0.501	0.524	0.551	0.424	0.607	0.522	0.466	0.414	0.554	0.491	0.455
Sample size $N = 1000$												
Random outliers contamination (4%)												
POL to HUB	1.034	0.928	0.847	0.817	1.018	0.94	0.92	0.888	1.037	0.905	0.899	0.886
POL to TUK	0.428	0.351	0.352	0.375	0.336	0.405	0.329	0.266	0.324	0.324	0.241	0.21
HUB to TUK	0.433	0.386	0.41	0.453	0.329	0.424	0.363	0.307	0.313	0.355	0.266	0.239

are generated through a day-ahead auction mechanism where equilibrium prices are obtained for each hour of next day. As different bids for each hour of next day are unknown when the auction takes place, it is then sensible to expect a stronger relation between prices observed at each hour of subsequent days, rather than between prices observed at different hours of the same day. Second, it has been proven that the forecasting performances of models built on hourly prices are better than those of models estimated on average daily prices (Raviv et al., 2015).

5.2. Preliminary adjustments and tests

Differences in load periods can cause significant variations in price time series. A first inspection, based on graphs, spectra and ACFs (see an example in Figure 1) for different hours, shows that the series have long-run behavior and annual dynamics, which change according with the load period. A common characteristic of price time series is the weekly periodic component (of period 7), suggested by the spectra that show three peaks at the frequencies 1/7, 2/7 and 3/7, and a very persistent autocorrelation function.

We assume that the dynamics of log prices can be represented by a nonstationary level component L_{th}, accounting for level changes and/or long-term behavior, and a residual stationary component p_{th}, formally, $\log P_{th} = L_{th} + p_{th}$.

To estimate L_{th} we used the wavelets approach (Percival & Walden, 2000). Wavelets have been used in many studies, including Trueck et al. (2007), Janczura & Weron (2010) and Lisi & Nan (2014). We considered the Daubechies least asymmetric wavelet family, LA(8), and the coefficients were estimated *via* the maximal overlap discrete wavelet transform (MODWT) method (for details, see Percival & Walden (2000)). The influence of positive and negative peaks on the estimation of L_{th}, has been minimized through an iterative procedure similar to that used by Nan et al. (2014) which ensures the robustness of the long-term estimation to the presence of spikes.

As an example of the time series of prices and corresponding estimated long-term component, Figure 2 shows P_{th} for four different hours, with the estimated nonstationary level component superimposed[8].

It is interesting to note the different volatility structure of the time series and how the presence and magnitude of jumps changes among hours.

[8]The remaining hours have not been reported for lack of space, but are available upon request.

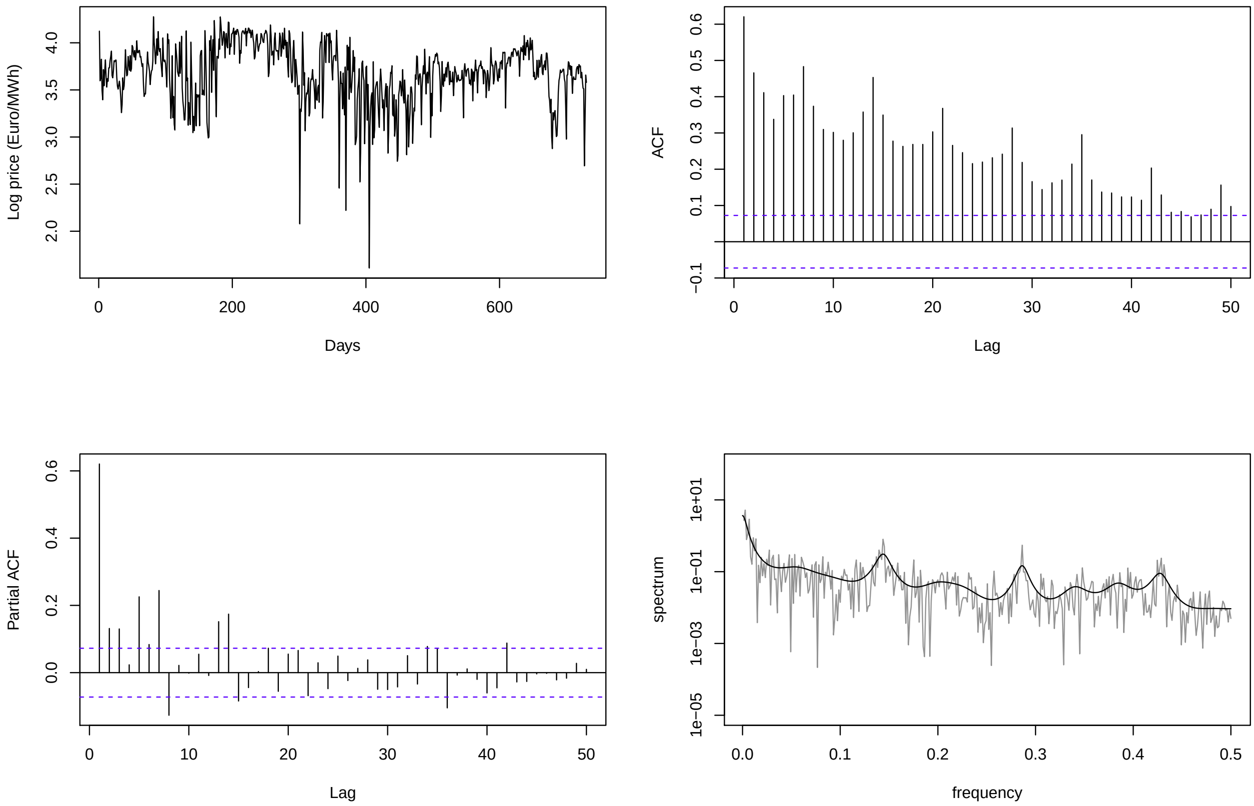

Figure 1: Time series of electricity log prices on the Italian market (hour 4) from 1/1/2013 to 12/31/2014. Autocorrelations functions (ACF and PACF) and periodogram are reported.

The time series obtained after the removal of the long-term component are stationary as it is confirmed by the application of robust and non-robust tests of unit root and stationarity. Table 5 reports the results of the application of three non-robust unit root tests, one non-robust stationarity test and one robust stationarity test. The non-robust unit-root tests are the augmented version of the Dickey-Fuller test (Said & Dickey, 1984), the Phillips-Perron test (Phillips & Perron, 1988) and the tests proposed by Elliott et al. (1996) using both the DF-GLS and the P statistics (ERS-DF-GLS and ERS-P, respectively). The stationarity test KPSS is applied both in its original non-robust version (Kwiatkowski et al., 1992) and in the robust version, recently introduced by Pelagatti & Sen (2013). The robust version of the test, based on ranks, has been computed using an auxiliary regression with 7 and 14 lags to take into account of the weekly seasonality of the data. From the table is possible to see that, using non-robust versions of the tests (first five lines of the table), conclusions could be controversial. For example, using the ADF test with constant, in

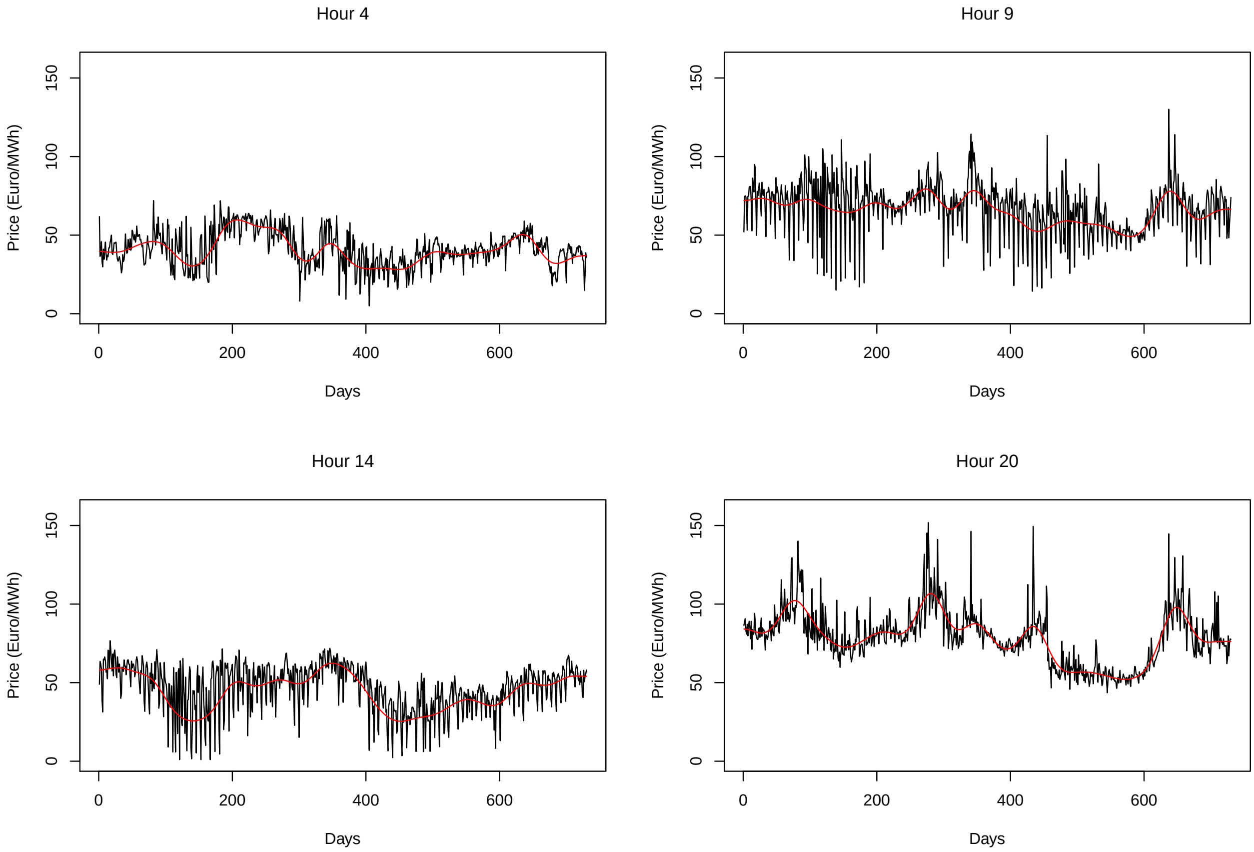

Figure 2: Long-run component (red line) estimated for four hours selected out of the total 24 hours of the sample.

four cases the hypothesis of a unit root is rejected, even on the original time series. According to the non-robust version of the KPSS test stationarity of the original series is not rejected in 8 cases at 5% significance level. When the robust version of the KPSS is used, results are coherent and close to what it is expected: stationarity is always rejected on the original time series and almost always accepted on the de-trended series[9].

Stationary time series obtained after the long-run behavior has been removed, are suitable for the estimation of threshold models. Of course, before moving to that step, we need to test that the nonlinear threshold process could be considered a better generation process then a simpler linear model (Misiorek et al., 2006; Chan et al., 2015). As reported by Chan & Ng (2004), nonlinearity of a time series can be confounded by the presence of outliers. For this reason we

[9]The tests reported in Table 5 are computed considering only a constant in the auxiliary regression, because when a linear trend has been introduced it has revealed not significant, almost in all cases.

Table 5: *Unit root and stationarity tests applied to original (log) and de-trended time series at 5% (first two columns) and 1% (last two columns) significance levels. Null hypothesis for ADF (Augmented Dickey-Fuller), PP (Phillips-Perron) and ERS (Elliot-Rothenberg-Stock) tests: presence of a unit root. Null hypothesis for KPSS (Kwiatkowski-Phillips-Schmidt-Shin, classic and robust version) tests: stationarity.*

	Number of rejections of the Null Hypothesis			
	Significance level: 0.05		Significance level: 0.01	
Type of Test	**Original**	**De-trended**	**Original**	**De-trended**
ADF	4	24	2	24
PP	24	24	24	24
ERS-DF-GLS	9	13	1	9
ERS-P	5	24	2	24
KPSS	16	0	13	0
Robust KPSS lag7	24	0	24	0
Robust KPSS lag14	24	0	21	0

applied, besides the classical F test by Tsay (1989), the robust version by Hung et al. (2009). To enhance the discriminative power of the F test in the presence of additive outliers, the Schweppe type of generalized-M (GM) estimator is considered with the polynomial weight function. Results of linearity vs. nonlinearity tests are shown in Table 6: the table reports the number of times (out of the total 24 series) the hypothesis of linear generating process is rejected using both the non robust (left panel) and the robust (right panel) version of the test. Different combinations of p and d have been considered, taking into account the empirical autocorrelation functions of p_{th} and the multilevel seasonality which is commonly shown by electricity spot prices (Janczura et al., 2013; Nowotarski et al., 2013). When daily time series of each hourly auction are analyzed, weekly frequency is the strongest source of seasonality also highlighted by the ACFs, thus, possible values of the two parameters go from 1 to 7. When the non-robust test is used, the nonlinearity hypothesis is more likely with low values of p, while the number of rejection increases with p when the robust test is applied. However, it is immediately clear that in the majority of the cases the linearity hypothesis is rejected and the nonlinear threshold process is likely to have generated the

Table 6: *F tests under the hypothesis of linearity. Number of cases the null hypothesis is rejected out of 24. Left panel: the* non robust *test by Tsay (1989) is applied. Right panel: the* robust *test by Hung et al. (2009) is applied. d is the lag of the threshold variable, p is the AR order of the model.*

	Tsay (1989) non-robust test							Hung *et al.* (2009) robust test						
$d \setminus p$	1	2	3	4	5	6	7	1	2	3	4	5	6	7
1	18	17	17	17	14	11	10	14	14	13	13	13	16	16
2	18	10	8	17	17	16	10	14	12	12	12	13	16	17
3	16	10	8	8	12	13	7	14	10	9	10	14	15	11
4	18	17	17	11	10	13	15	12	15	15	13	14	14	16
5	12	13	12	14	13	10	8	9	13	12	12	12	11	6
6	9	9	11	13	13	15	15	13	17	17	17	16	8	10
7	22	16	15	14	13	11	12	15	15	18	16	16	14	13

observed trajectories, particularly when p goes to 7 and the robust test is applied.

After removing the long-term component and getting, as a result, the stationary time series p_{th}, we are ready to estimate a SETAR(p,d) model with exogenous regressors, as reported in equation (1). The order of the model (parameters p and d) has been selected applying two robust versions of the Akaike Information Criteria (AIC). The first proposal is based on the formula (3.8) in Franses & van Dijk (2000) for the calculation of the AIC for a 2-regime SETAR model: in our case, the variances of the regimes are calculated from the polynomial weighted residuals obtained with the robust estimation of the SETAR model. The second robust AIC proposal is contained in the paper by Tharmaratnam & Claeskens (2013) who introduce a modified information criteria based on standardized residuals obtained from MM estimates of autoregressive and scale parameters (see equation 13 of Tharmaratnam & Claeskens, 2013 and A.1 in its appendix). This AIC has been adapted for each regime to the results of the present paper by replacing the estimates with polynomial weighted estimates. The corresponding results are reported in Table 7 where the top panel refers to our first robust AIC and the bottom panel contains the output of the second robust AIC. In order to summarize the results on the 24 hours, values have been first normalized between 0 and 1 for each hour and then averaged over the 24 hours. Looking at both panels, the minimum values are observed when the threshold is estimated on y_{t-1} ($d = 1$) and the 6 AR parameters are included ($p = 6$). The second minimum value is observed when $d = 1$ and $p = 7$. As prices are collected 7 days a week, weekly seasonality is more likely to be captured with $p = 7$. For this reason, a SETAR(7,1) can be considered the best generating process.

5.3. Forecasting day-ahead prices

In section 4 we have compared the bias of different estimators of SETAR models and the superiority of robust GM-estimator (POL and HUB) has been shown and the polynomial function has been selected as the best performer. In this section, we want to compare the forecasting performances of the polynomial to those of the LS non-robust estimator.

Starting from a simple AR(7) model, which can be thought as the benchmark model, we compare the forecasting performances of the polynomial and the LS estimator, gradually increasing the complexity of the model. Thus, the basic model contains only autoregressive components, excluding the matrix $\mathbf{Z}$ reported in equation (1).

Remembering what has been said at the beginning of this section, the period 2013-2014 has been used to estimate the first model, then a set of day-ahead predictions is obtained for year 2015 applying a rolling-window procedure (see, for instance, Gianfreda & Grossi, 2012).

To this aim, we generate 365 one day-ahead forecasts $\hat{p}_{t+1}$ for each model estimated on a 2-year long rolling window. Predictions of the observed spot prices are given by $\hat{P}_{t+1} = \exp(\hat{L}_{t+1} + \hat{p}_{t+1})$, where $\hat{L}_{t+1} = \hat{L}_t$, which means that we use the estimated level value in t as a prediction for $t + 1$. Besides its simplicity, this assumption is motivated by the small short-term variability of the long-term component which, by definition, should be basically the same for two contiguous days. We acknowledge, as proved by Nowotarski & Weron (2016) that the long-term seasonal component is very important in forecasting electricity prices, but this term has already been incorporated in the long-run component estimated by the wavelet approach.

As it is well known, the forecasting ability of models can be influenced by yearly seasons and the presence of spikes can vary from season to season. For this reason, the comparison is done not only for the whole year but also for each single season (winter: January-March, spring: April-June, summer: July-September, autumn: October-December).

The prediction ability of different models is evaluated using two different prediction error statis-

Table 7: *Robust AIC for different combinations of parameters p (columns) and d (rows). Values in the table are normalized between 0 and 1 for each hour and then averaged over the 24 hours.*

Robust AIC based on polynomial weighted estimates							
$d \setminus p$	1	2	3	4	5	6	7
1	0.488	0.378	0.330	0.338	0.319	0.208	0.265
2	0.591	0.548	0.542	0.510	0.417	0.359	0.313
3	0.729	0.737	0.494	0.497	0.491	0.366	0.380
4	0.677	0.782	0.634	0.518	0.509	0.360	0.342
5	0.698	0.793	0.711	0.655	0.500	0.390	0.383
6	0.671	0.774	0.735	0.700	0.606	0.415	0.360
7	0.683	0.767	0.721	0.694	0.662	0.547	0.418

Robust AIC based on MM estimates							
$d \setminus p$	1	2	3	4	5	6	7
1	0.564	0.498	0.475	0.447	0.452	0.323	0.344
2	0.647	0.568	0.584	0.563	0.485	0.410	0.419
3	0.636	0.705	0.564	0.563	0.537	0.422	0.376
4	0.668	0.699	0.682	0.514	0.541	0.398	0.345
5	0.652	0.708	0.630	0.599	0.541	0.406	0.442
6	0.686	0.702	0.669	0.672	0.575	0.451	0.422
7	0.665	0.695	0.634	0.654	0.649	0.526	0.419

tics: the Mean Square Error (MSE) and the Mean Absolute Error (MAE)[10]. The comparison between pairs of models is tested by means of statistical tests. The most common tests are the Diebold and Mariano's test (D-M) (Diebold & Mariano, 1995) and the Model Confidence Set test (MCS) (Hansen et al., 2003, 2011). In this paper the 1-tailed version of the Diebold-Mariano and MCS test at 5% significance level are used, considering the MSE and MAE loss functions.

In Table 8 and 9 a simple AR(7) model is compared with a SETAR(7,1), when both LS and Polynomial (POL) estimators are applied. Table 8 reports the number of times (out of the total 24 hours) the AR outperforms the SETAR model. Table 9 shows results for the opposite case. In the last row of the tables, the fraction of cases in which one model is better than the other (out of the 120 cases[11]) is computed. Summing up the numbers of the last row in the two tables we get 100 for MSE and MAE, while the result is lower than 100 for the two tests (D-M and MCS test) because only significant cases are included. For instance, looking at row labeled "Whole" in Table 8, we argue that in 7 hours (load periods) the AR(7) estimated by LS performs better than the SETAR(7,1), estimated by LS, when the day-ahead forecasts for the whole year are included in the computation of MSE. Of course, the number in the same position, but in Table 9 is the complement to 24, that is 17. If we stay on the same row ("Whole") but focus on the D-M test columns, we find that just in 2 cases the forecasting performance of the AR(7) model is significantly better than the performance of the SETAR(7,1) using the MSE as loss function and the LS estimator. The number found in the same position, but in Table 9 is not the complement of 2 to 24, but 7, meaning that in 7 load periods the SETAR is significantly better than the AR model. In the remaining cases $(24 - 7 - 2 = 15)$ none of the two models significantly outperforms the other. Focusing on the last line of both tables is possible to conclude that the nonlinearity of SETAR model enables to better predict electricity prices in most of the cases, thus confirming the output of nonlinearity tests (see Table 6).

Tables 10 and 11 compare the forecasting ability of the LS and POL estimator of the basic SETAR(7,1) model, without external regressors. The superiority of the robust estimator (POL) is quite clear, particularly when all days of the year are included. In this case, in 22 cases the

[10]We didn't use the "percentage" version of MSE and MAE because in 2015 prices very close to zero was observed which could heavily bias the values of MSPE and MAPE.

[11]The total number of possible cases is given by $24 \times 5 = 120$, where 24 is the number of load periods in a day and 5 is the sum of the four seasons and the whole year.

Table 8: *Number of cases AR model gives better results than SETAR model (four seasons and whole year 2015), LS and POL estimation. Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at 5% significance level, MSE and MAE loss functions.*

	PES Ratios				**D-M test**				**MCS test**			
	MSE		**MAE**		**MSE**		**MAE**		**MSE**		**MAE**	
Period	LS	POL	LS	POL	LS	POL	LS	POL	LS	POL	LS	POL
Jan-Mar	8	10	8	9	0	3	2	2	0	1	1	1
Apr-Jun	12	14	6	16	0	3	0	3	0	1	0	2
Jul-Sep	6	3	6	3	1	1	0	1	0	0	0	0
Oct-Dec	7	7	7	7	1	1	1	1	0	0	1	0
Whole	7	7	5	7	2	1	1	0	0	0	0	0
Totals (120 cases)	33.33%	34.17%	26.67%	35.00%	3.33%	7.50%	3.33%	5.83%	0.00%	1.67%	1.67%	2.50%

Table 9: *Number of cases SETAR model gives better results than AR model (four seasons and whole year 2015), LS and POL estimation. Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at 5% significance level, MSE and MAE loss functions.*

	PES Ratios				**D-M test**				**MCS test**			
	MSE		**MAE**		**MSE**		**MAE**		**MSE**		**MAE**	
Period	LS	POL	LS	POL	LS	POL	LS	POL	LS	POL	LS	POL
Jan-Mar	16	14	16	15	4	2	6	2	2	0	5	1
Apr-Jun	12	10	18	8	5	1	5	1	1	0	2	1
Jul-Sep	18	21	18	21	12	10	9	11	6	7	7	8
Oct-Dec	17	17	17	17	6	10	6	7	3	5	3	4
Whole	17	17	19	17	7	9	10	9	7	6	7	7
Totals (120 cases)	66.67%	65.83%	73.33%	65.00%	28.33%	26.67%	30.00%	25.00%	15.83%	15.00%	20.00%	17.50%

Predictor Error Statistics (MSE and MAE) of POL are lower than those of LS and in 14 cases the performance of POL is significantly better than that of LS applying the Diebold-Mariano test (Table 11). The preference for the robust estimator on LS is not so clear in spring (April-June period), but this is due to the low presence of spikes in that time span and confirms the higher efficiency of LS with respect to robust estimators for uncontaminated series (see section 4).

Table 10: *SETAR model: number of cases LS model gives better results than POL model (four seasons and whole year 2015). Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at* 5% *significance level, MSE and MAE loss functions.*

	PES Ratios		**D-M test**		**MCS test**	
Period	**MSE**	**MAE**	**MSE**	**MAE**	**MSE**	**MAE**
Jan-Mar	12	5	1	0	0	0
Apr-Jun	6	6	0	0	0	0
Jul-Sep	4	5	0	0	0	0
Oct-Dec	5	5	1	1	0	1
Whole	2	2	0	0	0	0
Totals (120 cases)	24.17%	19.17%	1.67%	0.83%	0.00%	0.83%

The superiority of the robust estimator is overwhelming when regressors are introduced.

In the literature on electricity price forecasting, the strong influence of exogenous regressor on model's forecasting performances has been widely discussed (Gianfreda & Grossi, 2012; Weron, 2014). For this reason, we need to draw our attention on the possibility to introduce regressors which could improve the forecasting ability of the model by catching the peculiarities of the market. With reference of the Italian market, and taking the availability of predicted exogenous regressors into account, the following set of regressors are introduced in the models:

- deterministic day-of-the-week dummy variables, that is D_k, with $k = 1, \dots, 6$;
- day-ahead predicted demand of electricity, made available by the Italian authority (GME);
- day-ahead predicted wind generation, made available by the Italian Transmission System

Table 11: *SETAR model: number of cases POL model gives better results than LS model (four seasons and whole year 2015). Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at 5% significance level, MSE and MAE loss functions.*

	PES Ratios		**D-M test**		**MCS test**	
Period	**MSE**	**MAE**	**MSE**	**MAE**	**MSE**	**MAE**
Jan-Mar	12	19	1	2	0	2
Apr-Jun	18	18	2	2	2	1
Jul-Sep	20	19	11	10	6	7
Oct-Dec	19	19	5	6	6	5
Whole	22	22	14	14	9	7
Totals (120 cases)	75.83%	80.83%	27.50%	28.33%	19.17%	18.33%

Operator (TSO) Terna.[12]

Tables 12 and 13 compare the predictive accuracy of LS and POL estimators for the complex model SETARX(7,1) containing the above exogenous regressors. In this model, matrix $\mathbf{Z}$ contains the detrended day-ahead predicted demand of electricity and the detrended predicted electricity generation by wind. As for the price series, the level component of the two forecasted regressors has been estimated using the wavelets approach. Comparing Table 11 to Table 13, the fraction of cases where the POL estimator significantly outperform the LS estimator moves from less than 30% to almost 50% when the D-M test on MAE is considered.

6. Conclusions

A robust approach to modelling and forecasting electricity prices is suggested. As it is well known, one of the main stylized facts observed on electricity spot markets is the presence of sudden departure of prices from the normal regime for a very short time interval. This particular pattern is usually called “spike”. While the literature on electricity prices has so far focused on the modelling and prediction of spikes, this paper has dealt with robust estimators of models

[12] `https://www.terna.it/en-gb/home.aspx`

Table 12: *SETAR with forecasted demand, dummies and forecasted wind generation: number of cases LS model gives better results than POL model (four seasons and whole year 2015). Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at* 5% *significance level, MSE and MAE loss functions.*

	PES Ratios		**D-M test**		**MCS test**	
Period	**MSE**	**MAE**	**MSE**	**MAE**	**MSE**	**MAE**
Jan-Mar	4	2	1	0	0	0
Apr-Jun	10	5	0	0	0	0
Jul-Sep	7	7	0	0	0	0
Oct-Dec	5	6	1	1	0	1
Whole	4	3	0	0	0	0
Totals (120 cases)	25.00%	19.17%	1.67%	0.83%	0.00%	0.83%

Table 13: *SETAR with forecasted demand, dummies and forecasted wind generation: number of cases POL model gives better results than LS model (four seasons and whole year 2015). Comparisons with prediction error statistics (PES) values and p-values for the 1-tailed Diebold-Mariano and MCS tests at* 5% *significance level, MSE and MAE loss functions.*

	PES Ratios		**D-M test**		**MCS test**	
Period	**MSE**	**MAE**	**MSE**	**MAE**	**MSE**	**MAE**
Jan-Mar	20	22	12	13	10	12
Apr-Jun	14	19	5	6	3	7
Jul-Sep	17	17	7	10	3	8
Oct-Dec	19	18	12	12	8	10
Whole	20	21	16	18	15	18
Totals (120 cases)	75.00%	80.83%	43.33%	49.17%	32.50%	45.83%

for electricity prices. Robust estimators are not strongly affected by the presence of spikes and are effective in the prediction of "normal" prices which are the majority of the data observed on electricity markets.

Another stylized fact observed on electricity markets is the nonlinear nature of the generating processes of prices. Threshold processes are particular nonlinear processes which could be robustly estimated through a generalization to dependent data of GM-estimator originally developed for independent data.

Different proposals could be found in the literature, applying GM-robust estimator to SETAR based on different weighting functions. However, the different proposals have never been deeply compared to decide which function gives the smaller bias under particular conditions.

For this reason, we have carried out a Monte Carlo experiment to compare LS and GM estimators, with different weighting functions, for SETAR models: the Tukey's function, originally proposed and studied by Chan & Cheung (1994), the Huber's function, studied by Zhang et al. (2009) and the polynomial function of Lucas et al. (1996) suggested in Giordani (2006). The main result is that the bias in the threshold parameter estimator, which has been observed in previous works, decreases when Huber's and Polynomial weighting functions are applied, when the sample size increases and for complex contamination patterns. However, when the features of the trajectories are more similar to what is observed on electricity markets, the polynomial function looks to be the best estimator.

The robust GM-estimator of SETAR processes based on the polynomial weights has been applied to forecast hourly day-ahead spot prices observed on the Italian market in the period 2013-2015. The long-run trend has been estimated using a wavelet-based procedure and the stationarity of the de-trended series has been verified through robust tests. The nonlinearity of the generating process has been robustly tested using non-robust and robust tests. Finally the order of the SETAR model has been selected by a robust version of the Akaike Information Criteria.

Using prediction error statistics (MSE and MAE) and forecasting performance tests (Diebold and Mariano test and Model Confidence Set test), the nonlinear process SETAR(7,1) has revealed more effective than a linear AR(7) in predicting prices for year 2015, confirming the output of the robust test for nonlinearity. Besides the information set given by the past observations, several exogenous variables can used to improve the forecasting performances of nonlinear models applied to electricity prices. Following recent literature (Cló et al., 2015; Ketterer, 2014), days-of-the-week dummy variables, predicted electricity demand and predicted wind power generation have been introduced as exogenous regressors in the SETAR(7,1) model on the Italian market.

The superiority of the forecasting performance of the robust on the LS estimator with exogenous regressor is overwhelming. The introduction of effective regressors, not only improve the forecasting power of the models, but the predictive ability of the robust estimator is significantly better than that of the LS estimator in more than 50% of the total cases.

It is remarkable to stress that on the Italian market very large prices are never observed and even the highest prices collected in the last years could not be strictly defined as "spikes" in the sense used in other papers (see, for instance, Haldrup et al., 2016) applied to the Nordpool market. However, the robust estimators have revealed very effective in improving the forecasting performances of the model. Moreover, the overwhelming superiority of the method for models with regressors has proven that robust estimators are particularly desirable when multivariate extreme observations happens although spikes in univariate time series are not so evident.

Future research will be devoted to the application of robust estimators to markets other than the Italian and to study the asymptotic properties of the robust polynomial estimator when larger samples are considered.

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Appendix A. Appendix

Table A.1: *Ratios of the RMSE of the GM estimate with polynomial weights to the LS estimate. 1000 MC simulations of time series with sample size 500 and outliers with magnitude* $\omega = 10$ *times the standard deviation of the processes. 3-outlier case*

True values				$\hat{\gamma}$	$\hat{\beta}_1$	$\hat{\beta}_2$
γ	β_1	β_2	d			
0	0.9	-0.1	1	1.23	0.136	1.799
0	0.9	-0.77	1	1.261	0.145	0.941
0	-0.5	-1	1	0.61	0.197	0.176
0	-1	-0.5	1	0.571	0.108	0.319
0	0.3	0.8	1	1.247	0.428	0.238
0	0.5	0.8	1	1.203	0.233	0.242
0	-0.3	0.8	1	0.975	0.749	0.267
0	-0.5	0.8	1	0.868	0.425	0.262
0	0.8	0.3	1	1.463	0.165	0.49
0	0.8	0.5	1	1.341	0.159	0.308
0	0.8	-0.3	1	1.251	0.185	0.917
0	0.8	-0.5	1	1.186	0.186	0.575
0.1	0.3	0.8	1	1.098	0.408	0.245
-0.1	0.3	-0.8	1	0.946	0.581	0.323
0	0.3	0.8	2	0.445	0.563	0.229
0	0.3	-0.8	2	0.344	0.348	0.203
0.1	0.3	0.8	2	0.496	0.485	0.239
-0.1	0.3	-0.8	2	0.32	0.357	0.19

Table A.2: *Ratios of the RMSE of the GM estimate with polynomial weights to the LS estimate. 1000 MC simulations of time series with sample size 500 and outliers with magnitude* $\omega = 10$ *times the standard deviation of the processes. Multiple-outlier case*

True values				$\hat{\gamma}$	$\hat{\beta}_1$	$\hat{\beta}_2$
γ	β_1	β_2	d			
0	0.9	-0.1	1	1.152	0.053	3.153
0	0.9	-0.77	1	1.123	0.052	0.715
0	-0.5	-1	1	0.552	0.106	0.081
0	-1	-0.5	1	0.591	0.067	0.16
0	0.3	0.8	1	0.899	0.297	0.085
0	0.5	0.8	1	0.938	0.165	0.088
0	-0.3	0.8	1	0.653	0.597	0.09
0	-0.5	0.8	1	0.568	0.345	0.086
0	0.8	0.3	1	1.456	0.073	0.312
0	0.8	0.5	1	1.347	0.075	0.166
0	0.8	-0.3	1	1.1	0.071	0.725
0	0.8	-0.5	1	1.032	0.074	0.397
0.1	0.3	0.8	1	0.873	0.304	0.089
-0.1	0.3	-0.8	1	0.776	0.286	0.181
0	0.3	0.8	2	0.319	0.352	0.099
0	0.3	-0.8	2	0.181	0.254	0.103
0.1	0.3	0.8	2	0.34	0.341	0.096
-0.1	0.3	-0.8	2	0.17	0.248	0.099

Table A.3: *Number of cases RMSEs of the GM estimation with polynomial weights are better than RMSEs of the LS estimation. 1000 MC simulations of time series with sample size 500 and outliers with magnitude* $\omega = 10$ *times the standard deviation of the processes.*

$\hat{\gamma}$	$\hat{\beta}_1$	$\hat{\beta}_2$
3-outlier case		
9	18	17
Multiple-outlier case		
12	18	17

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